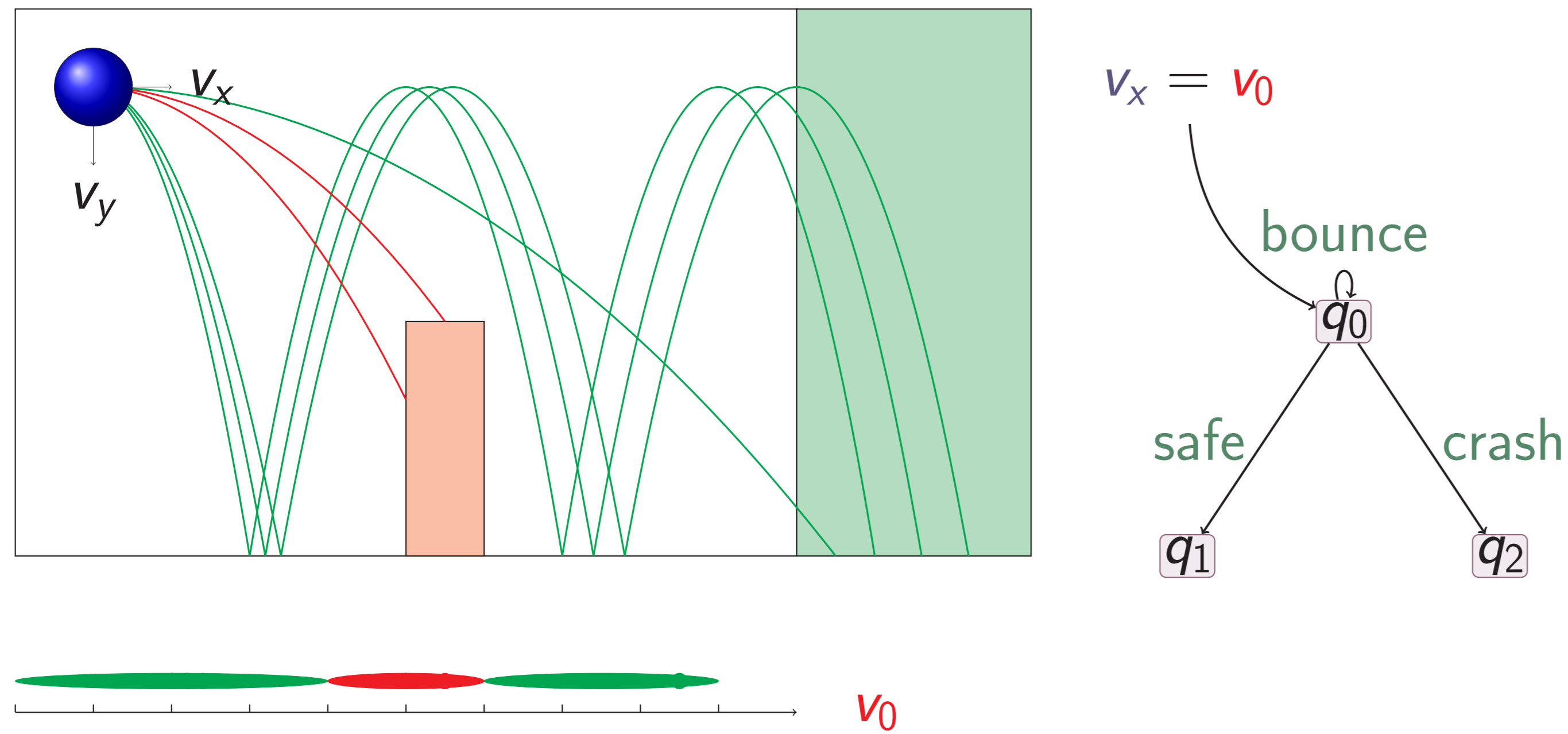


### An Example of Hybrid System: The Bouncing Ball

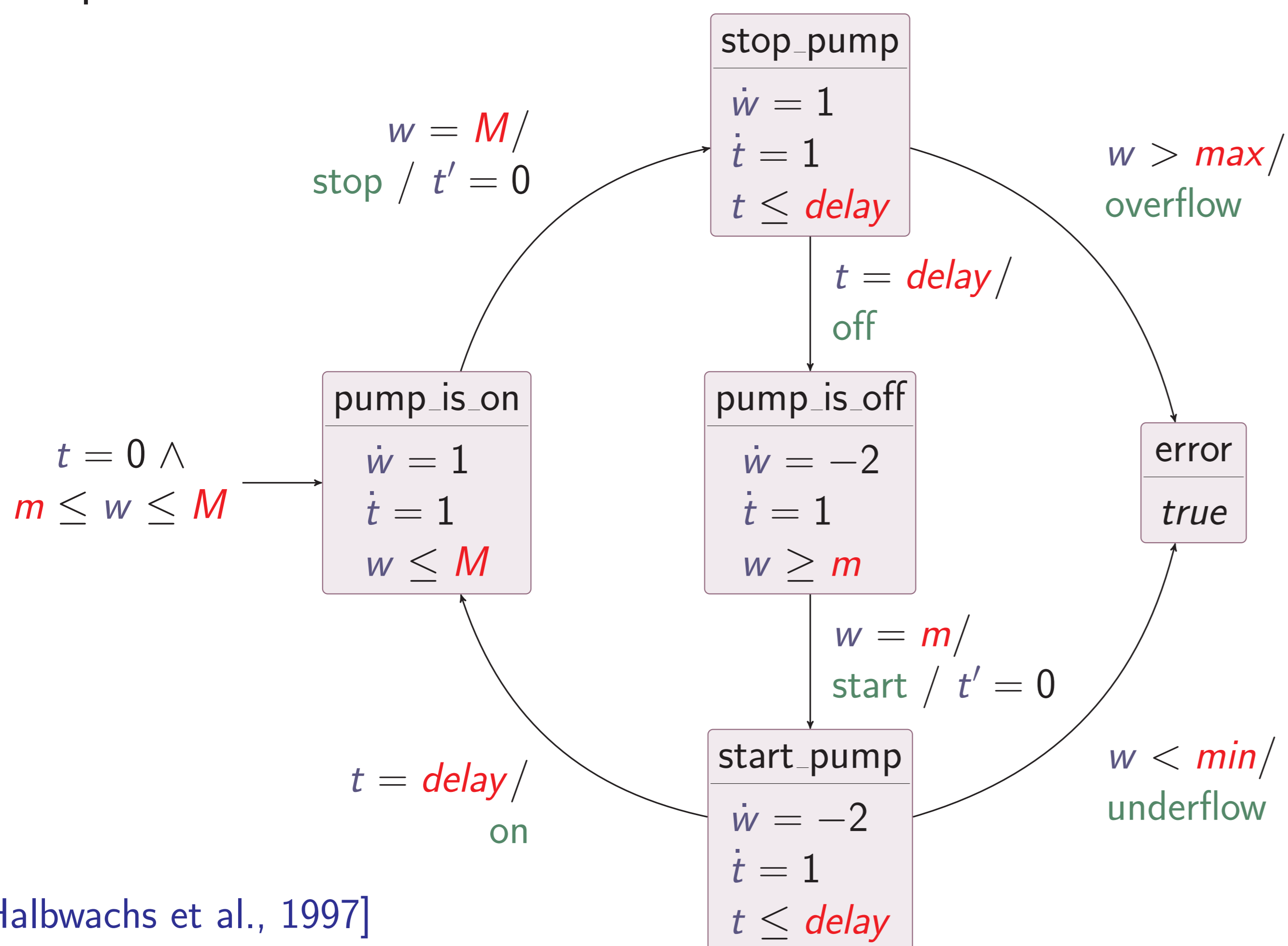
Hybrid systems combine

- ▶ Discrete behavior
- ▶ Continuous behavior

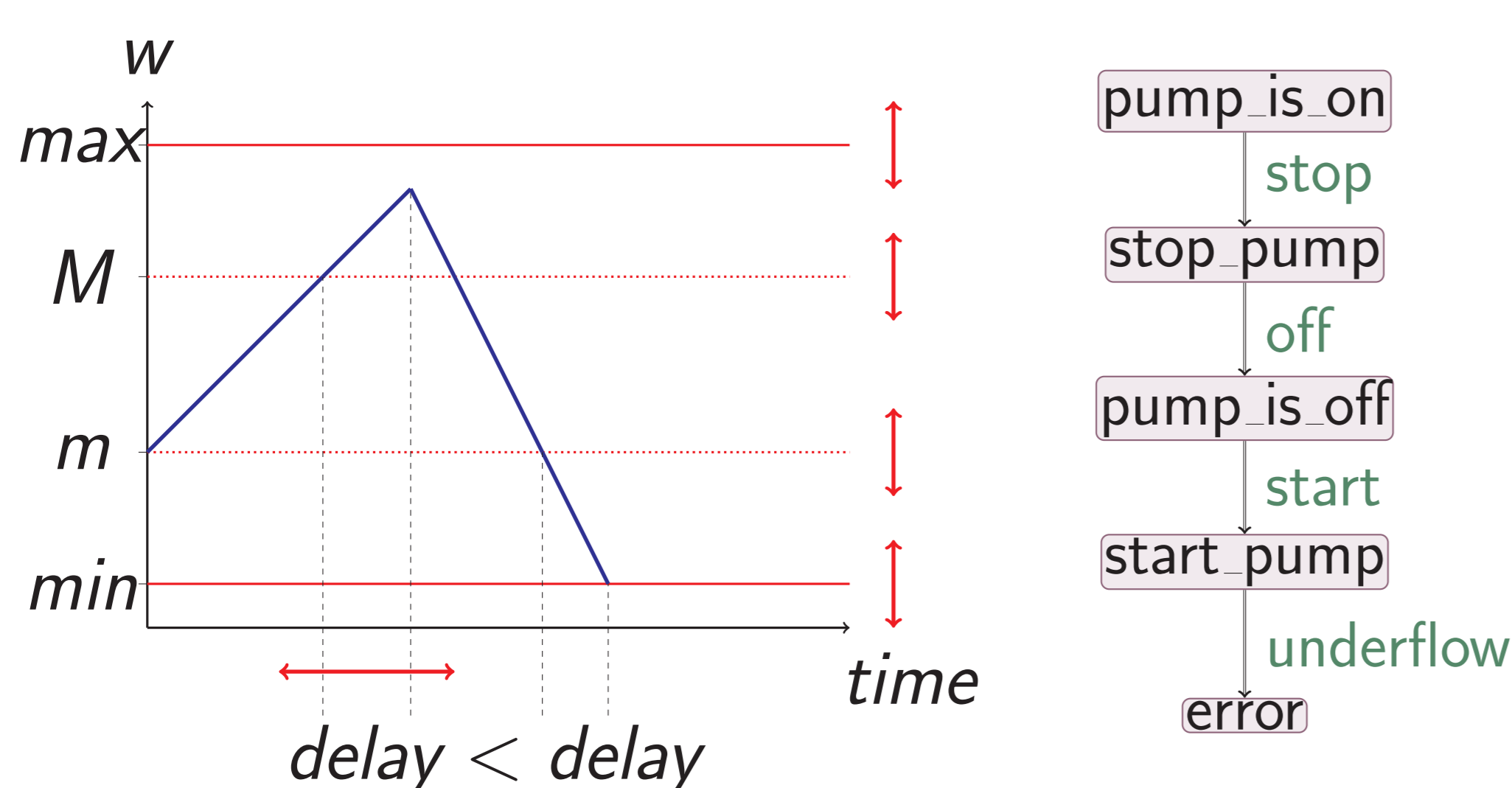


### Parameterized Hybrid Automata

- ▶ Hybrid Automata (HA): Sets of variables, actions, locations, and discrete transitions
- ▶ Parameterized Hybrid Automata: HA augmented with a set of parameters (unknown constants)
- ▶ Example: Water Tank



### The Parameter Synthesis Problem



- ▶ How to choose  $\min$ ,  $\max$ ,  $m$ ,  $M$  and  $\text{delay}$ , such that always  $\min < w < \max$ ?

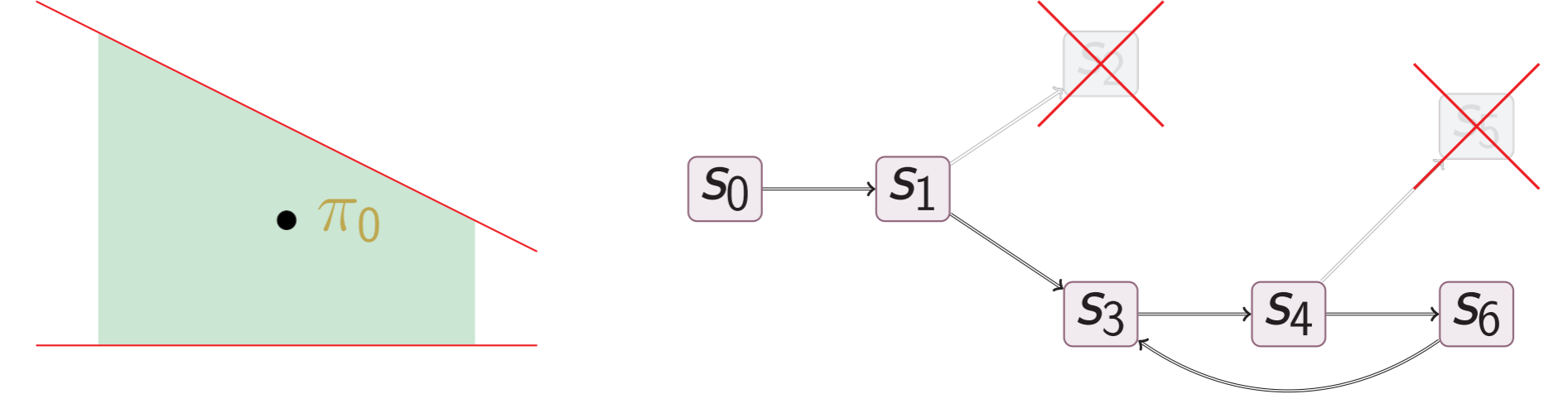
Synthesis problem: “find values for the parameters such that the system behaves well”.

We will synthesize here a constraint, viz., a convex and dense set of values.

### Parameter Synthesis for Hybrid Automata

- ▶ Inverse Method [Fribourg and Kühne, 2011]

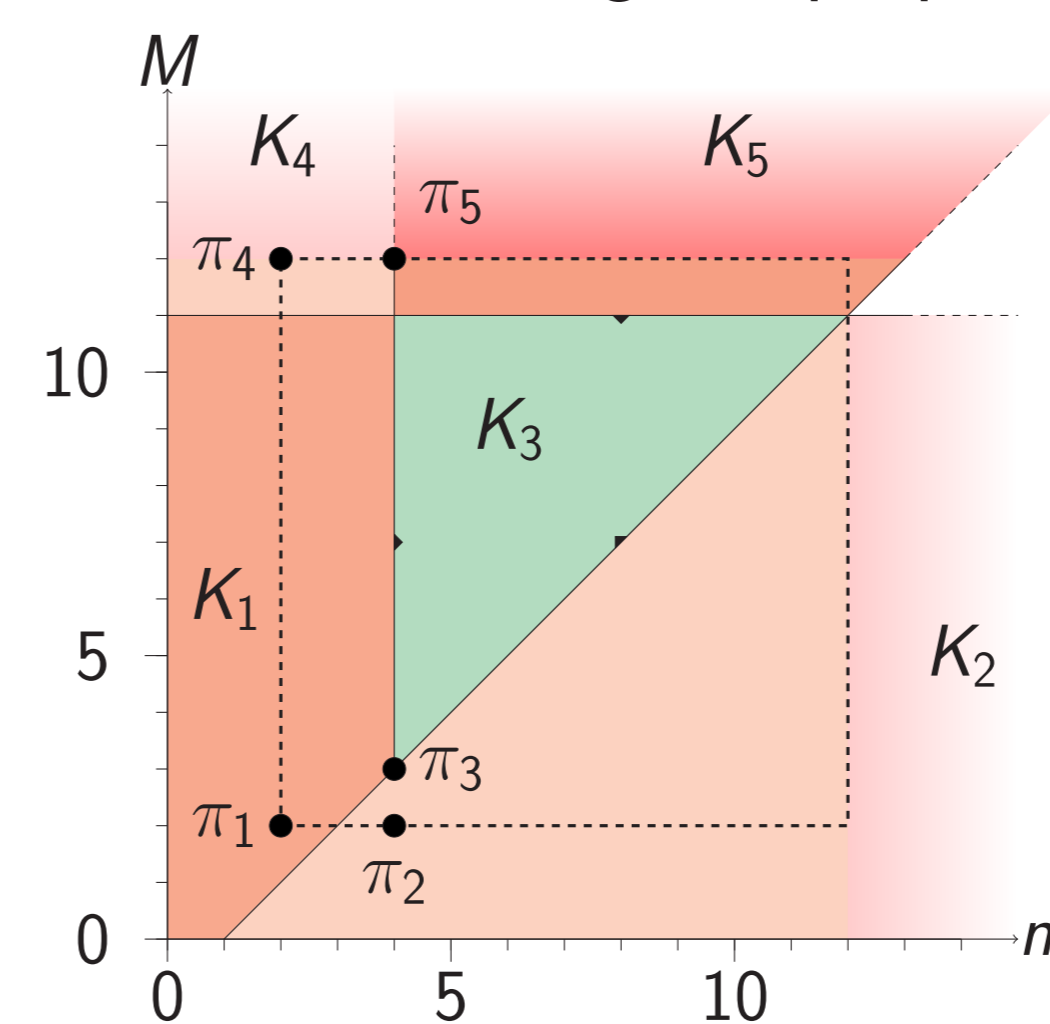
- ▶ Given an HA and a reference valuation  $\pi_0$  for the parameters, synthesize a constraint  $K_0$  guaranteeing the same time-abstract behavior as for  $\pi_0$



- ▶  $K_0$  obtained by iterative removal of states incompatible with  $\pi_0$

- ▶ Behavioral Cartography [André and Fribourg, 2010]

- ▶ Performs a tiling of the parametric space, and partition it between good and bad tiles w.r.t. a given property



Example of “good” constraint for the water tank:

$$M + \text{delay} \geq m \wedge m \geq \min + 2 \cdot \text{delay} \wedge \max \geq M + \text{delay}$$

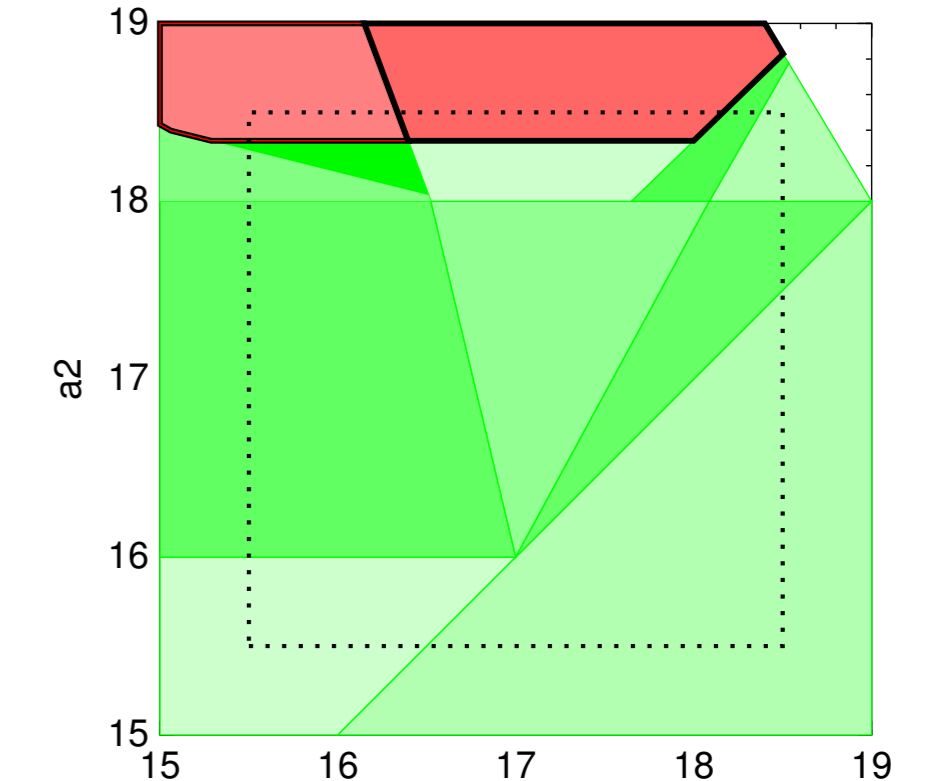
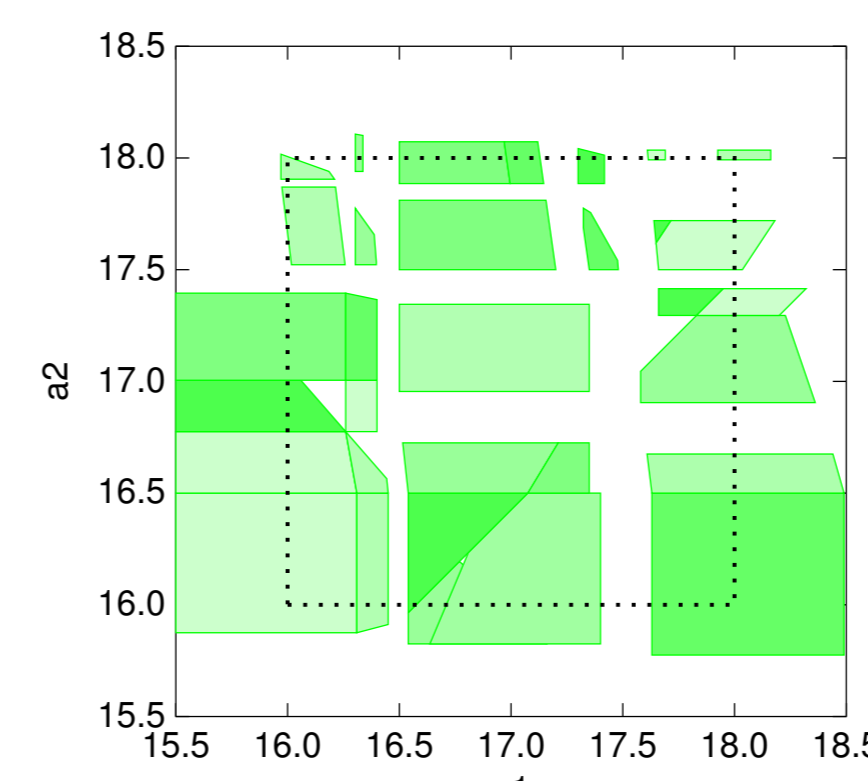
### Features of HyMITATOR

- ▶ Algorithms of Parameter Synthesis for Hybrid Systems

- ▶ Implements the inverse method and the behavioral cartography
- ▶ Includes local partitioning with linear over-approximations
- ▶ Makes use of predicate abstraction techniques
- ▶ Features an efficient merging technique [André et al., 2012]

- ▶ User-friendly Features

- ▶ Numerous options for analysis
- ▶ Graphical output



- ▶ Implementation [André and Kühne, 2012]

- ▶ Implemented in OCaml, using the Parma Polyhedra Library

### Try it!

- ▶ Distributed under the GNU General Public License
- ▶ [www.lsv.ens-cachan.fr/Software/hymitator/](http://www.lsv.ens-cachan.fr/Software/hymitator/)

### References

- ▶ André, É. and Fribourg, L. (2010). Behavioral cartography of timed automata. In *RP'10*, volume 6227 of *LNCS*, pages 76–90. Springer.
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- ▶ Fribourg, L. and Kühne, U. (2011). Parametric verification and test coverage for hybrid automata using the inverse method. In *RP'11*, volume 6945 of *LNCS*, pages 191–204. Springer.
- ▶ Halbwachs, N., Proy, Y.-E., and Roumanoff, P. (1997). Verification of real-time systems using linear relation analysis. *Formal Methods In System Design*, 11(2):157–185.