

## Internship Proposal

# Bounded model checking for energy-aware real-time systems

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## Context

Real-time systems have become ubiquitous in the past few years. Some of them (automated plane and unmanned systems control, banking systems, etc.) are critical in the sense that no error must occur. Testing these systems can possibly detect the presence of bugs, but not guarantee their absence. It is thus necessary to use formal methods such as model checking [BK08] so as to prove formally the correctness of such a system.

Formal verification provides mathematically rigorous guarantees that system behaviors satisfy desired safety and correctness properties, which is crucial for detecting subtle errors that testing alone may miss. Often, critical systems feature key continuous variables, such as time, but also energy. Timed automata [AD94] extend classical automata with clocks, enabling precise modeling of real-time constraints, while weighted or energy timed automata [Bac+21] further incorporate quantitative resources such as energy consumption or production, making them well-suited for analyzing energy-critical systems.

## Subject

In the context of verification of timed systems, **bounded model checking** [Sor02; KJN12; WZZ17] is valuable because it efficiently explores behaviors within a finite horizon, allowing rapid detection of counterexamples and scalable analysis of complex, resource-constrained models. Even better, bounded model checking can be applied to classes of systems where infinite-horizon analyses are usually undecidable [KP12].

The objective of this internship is to **design algorithms for bounded model checking of timed automata extended with energy variables**, allowing answer to questions such as “given an autonomous vehicle equipped with both a chargeable battery and a solar panel, what is the minimal energy needed to perform a certain itinerary in less than  $k$  steps?” Or to answer security-related questions such as: “by looking at the final percentage of charge of the battery of an autonomous

vehicle, can an attacker infer secret information (such as the maximum speed, or geographic information) over the vehicle in the past  $k$  steps?”

The analyses will be carried for both well-established timed automata [AD94] and the recent formalism of automata with timers [Bru+23]. Depending on the time and interest of the applicant, an implementation may be carried out using solvers.

## Keywords

Formal methods, model checking, real-time systems, energy-aware systems

## Skills

The following skills are not compulsory, but would be welcome:

- formal methods;
- timed automata;
- SMT/SAT solvers.

## Location and environment

Highly motivated applicants are being sought. The internship will take place at **École Centrale Nantes**, within Nantes Université. LS2N is an internationally recognized research laboratory comprising over 450 scientists.

Nantes combines a lively, student-friendly atmosphere with a rich scientific and cultural scene, making it a great place to learn, research, and enjoy everyday life.

## References

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Version: December 4, 2025