

# Conformance testing for input/output symbolic transition systems

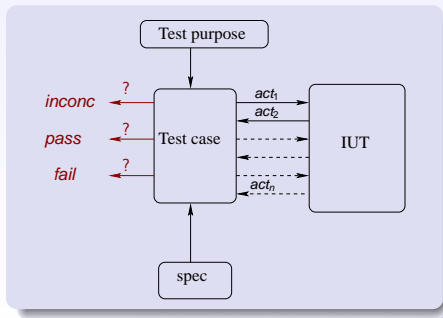
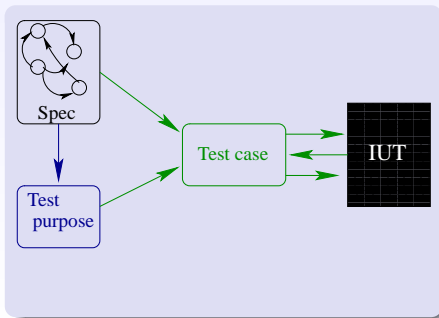
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# Conformance testing for reactive systems : “model-based testing”

- **Spec** : automata based description of expected behaviours
- **IUT** : “black-box view” of the implementation under test
- **Test purpose** : selected behaviours from Spec to be the test target (expertise)
- **Test case** : verdict computation by analysis of traces  
 $t = act_1 act_2 \dots act_n$  observed on IUT



## Hypotheses

- Spec defines a set of models by means of a conformance relation *conf*

$$MOD(Spec) = \{i \in MOD \mid i \text{ conf } Spec\}$$

- IUT is a “black-box” which can be modelled by a model  $i_{IUT}$

$$\forall IUT, \exists i_{IUT} \in MOD, \forall t \in Traces, t \in Tr(IUT) \iff t \in Tr(i_{IUT})$$

## Goal of a testing method

- recognise  $i_{IUT}$  among all the possible models in MOD
- Correctness (non bias) and completeness (exhaustivity)

# Symbolic transition systems

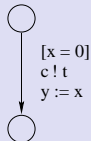
Input/Output symbolic system transitions :

- Finite representation of large or infinite state-based systems
- Data are exchanged in input/output messages

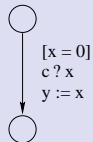
## Transitions

- Guards on attribute variables
- emission/reception of data on a channel
- state modification

## Emission of a message denoted by a term



## Reception of a message on an attribute variable



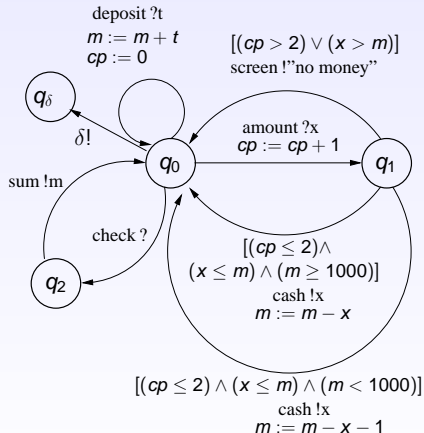
# Input/Output Symbolic Transition Systems : IOSTS

$G = (Q, q_0, Trans)$

- $Q$  set of states
- $q_0$  initial state
- $Trans$  set of transitions

Enrichment by quiescence

- source state  $q$
- action : emission  $\delta!$
- guard :  $\bigwedge_e (\neg guard_e)$  for all emissions  $e$  of source  $q$
- substitution  $id$
- target state : state  $q_\delta$



# Our goal

- defining appropriate test purposes Obj
- proposing selection criteria for test purposes
- Algorithm for selecting data in order to stimulate IUT with respect to Obj and emitting a verdict.
- Which verdicts ?
  - ① **PASS** IUT satisfies Obj
  - ② **FAIL** IUT does not conform to Spec
  - ③ **INCONC** IUT does not satisfy to Obj but conforms to Spec
  - ④ **WeakPASS** IUT not only satisfies Obj but also satisfies some other behaviours of Spec
- Non determinism in Spec  $\Rightarrow$  verdicts INCONC, WeakPASS

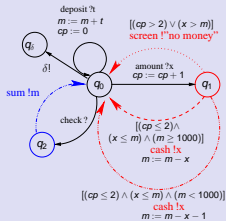
Our approach : using **Symbolic execution technique**

Symbolic execution tree = description of all expected behaviours

a symbolic path = *an intensional class of similar concrete behaviours*

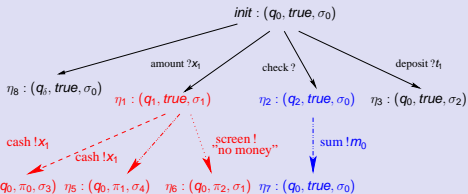
# Symbolic execution

## IOSTS



## Symbolic state $(q, \pi, \sigma)$

- $q$  state
- $\pi$  path predicate
- $\sigma$  assignment of attribute variables by using symbolic variables



$$\begin{aligned} \sigma_3 &= x \rightarrow x_1, m \rightarrow m_0 - x_1, t \rightarrow t_0, cp \rightarrow cp_0 + 1 \\ \sigma_4 &= x \rightarrow x_1, m \rightarrow m_0 - x_1 - 1, t \rightarrow t_0, cp \rightarrow cp_0 + 1 \\ \sigma_1 &= x \rightarrow x_1, m \rightarrow m_0, t \rightarrow t_0, cp \rightarrow cp_0 + 1 \end{aligned}$$

$$\begin{aligned} \pi_0 &= (cp_0 + 1 \leq 2) \wedge (x_1 \leq m_0) \wedge (m_0 \geq 1000) \\ \pi_1 &= (cp_0 + 1 \leq 2) \wedge (x_1 \leq m_0) \wedge (m_0 < 1000) \\ \pi_2 &= (cp_0 + 1 > 2) \vee (x_1 > m_0) \end{aligned}$$

# Conformance testing

## *IUT ioco Spec*

$\forall tr \in Trace(Spec) \cap Trace(IUT)$  if it exists  $c!v$  such that  $tr.c!v \in Tr(IUT)$ , then  $tr.c!v \in Tr(Spec)$

## “input enable” hypothesis

IUT accepts all inputs in all states

## Test purpose

Finite subtree of the symbolic execution tree

- leaves labelled by the key word *accept*
- intermediate nodes labelled by the key word *skip*

## Observable traces between the test case and IUT

- Messages sent to IUT :  $stim(c?t)$  [stimulations/controllability]
- Messages sent by IUT :  $obs(c!t)$  [observations]



## Goal of test execution :

- depending on (the beginning of) the trace, computing the possible current states of the IUT according to Spec
- computing concrete stimulations in order to aim an accept state (given by the test purpose) or to produce a verdict

## Description of a possible current state = a context as $(\eta, \varphi)$

- $\eta$  symbolic state
- $\varphi$  predicate on symbolic variables (of symbolic execution tree) taking into account the first elements of the testing trace between the test case and IUT

# Principle of the algorithm

SC : set of current contexts

- Initial set of contexts :  $SC_0 = \{(q_0, true)\}$
- Steps of the algorithm expressed by rules of the form :

$$\frac{SC}{Result} \quad cond$$

with :

- *cond* set of conditions including  $stim(act)$  or  $obs(act)$

Notation :  $SC \xrightarrow{act} Result$

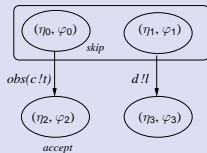
- *Result* of the form
  - a new current set of contexts
  - or a verdict among PASS, FAIL, WeakPASS and INCONC

Testing trace :  $[act_1, act_2, \dots, act_n \mid Verdict]$

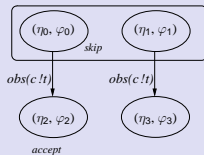
$$SC_0 \xrightarrow{act_1} SC_1 \xrightarrow{act_2} SC_2 \dots SC_{n_1} \xrightarrow{act_n} Verdict$$

# Verdicts

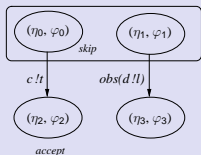
## PASS



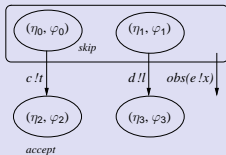
## WeakPASS



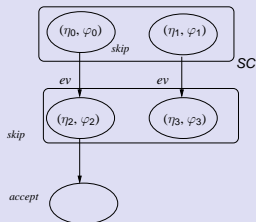
## INCONC



## FAIL



# Auxiliary functions



$$\text{Next}(ev, SC) = \{(\eta_2, \varphi_2), (\eta_3, \varphi_3)\}$$

$$\text{NextSkip}(ev, SC) = \{(\eta_2, \varphi_2)\}$$

$$\text{NextPass}(ev, SC) = \emptyset$$

With  $\Delta \in \{?, !\}$ , if

- $\eta_0 = (q, \pi, \sigma)$
- $\eta_2 = (q', \pi', \sigma')$
- $(\eta_0, c\Delta u, \eta_2)$  transition of symbolic execution tree
- $ev$  is  $c\Delta t$  (resp.  $c\Delta$ )

then

- $\varphi_2$  is  $\varphi_0 \wedge (t = u)$  (resp.  $\varphi_0$ )
- and  $\varphi_2 \wedge \text{targetCond}(\eta_2)$  is satisfiable where  $\text{targetCond}(\eta_2)$  is

$\bigvee \quad \pi$   
 $\pi$  path condition  
of an *accept* state  
reachable from  $\eta_2$

# Rules for the observations ( $ev$ of the form $c!t$ or $c!$ )

**Rule 1** : Emission compatible with Obj but no *accept* is reached.

$$\frac{SC}{Next(ev, SC)} \quad obs(ev), NextSkip(ev, SC) \neq \emptyset, NextPass(ev, SC) = \emptyset$$

**Rule 2** : Emission not expected with respect to Spec

$$\frac{SC}{FAIL} \quad obs(ev), Next(ev, SC) = \emptyset$$

**Rule 3** : Emission not compatible with Obj, but compatible with Spec

$$\frac{SC}{INCONC} \quad obs(ev), Next(ev, SC) \neq \emptyset, NextSkip(ev, SC) = \emptyset$$

**Rule 4** : All next contexts are *accept* ones.

$$\frac{SC}{PASS} \quad obs(ev), Next(ev, SC) = NextPass(ev, SC), Next(ev, SC) \neq \emptyset$$

**Rule 5** : Some next contexts are *accept* ones, but not all of them

$$\frac{SC}{WeakPASS} \quad obs(ev), NextPass(ev, SC) \neq \emptyset, NextPass(ev, SC) \subsetneq Next(ev, SC)$$

**Rule 6** : Stimulation of the *SUT* (*ev* of the form  $c?t$  or  $c?$ )

$$\frac{SC}{Next(ev, SC)} \quad stim(ev), NextSkip(ev, SC) \neq \emptyset$$

Initialisation rule (**Rule 0**)

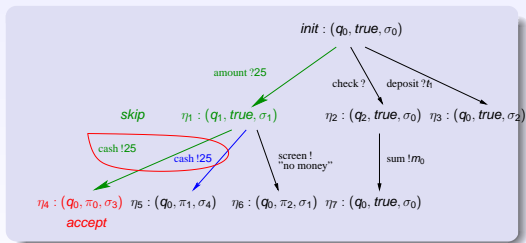
$$\overline{\{(init, true)\}}$$

# Illustration : *WeakPASS* verdict

Trace *amount?25 cash!25*

$SC_0 = \{(init, true)\} \xrightarrow{amount?25} SC_1 = \{(\eta_1, (x_1 = 25))\} \xrightarrow{cash!25} WeakPASS$

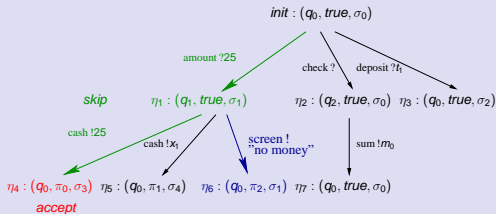
Current set of contexts after *cash!25* contains two contexts, but only one has a state lallebed by *accept*



# Illustration : INCONC verdict

Trace *amount?25 screen!"nomoney"*

$$SC_0 = \{(init, true)\} \xrightarrow{\text{amount?25}} SC_1 = \{(\eta_1, (x_1 = 25))\} \xrightarrow{\text{screen!"nomoney"}} INCONC$$

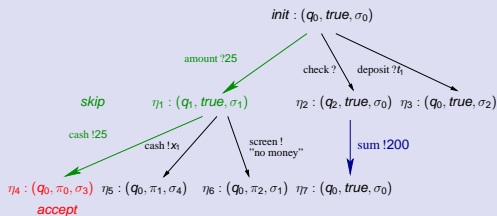




# Illustration : FAIL verdict

Trace *amount?25 sum!200*

$$SC_0 = \{(init, true)\} \xrightarrow{amount?25} SC_1 = \{(\eta_1, (x_1 = 25))\} \xrightarrow{sum!200} FAIL$$



## Correctness and completeness

### Inclusion criterion

- End of the computation of the symbolic execution tree when a redundancy is detected :  
all concrete values of the new encountered symbolic state are included in the one of a previous computed one
- Good candidate for the selection of test purposes

### Implementation within the AGATHA tool (CEA)

- Need a strategy to apply rules
- Decision procedure (inclusion criterion) and constraint solving (stimulation computation) in the Presburger arithmetic (Omega Library)

## Design

- Reactive systems described by synchronous composition of IOSTS

$$Spec = Spec1 \times Spec2$$

⇒ compositional testing

- Incremental design by refinement

*ConcreteSpec refines AbstractSpec*

⇒ refinement testing

# Compositional testing : $Spec = Spec1 \times Spec2$

## Intuition

intensively testing each component according to the operational profile of the global system  
(some behaviours are priviledged while others cannot be performed)

## Key points

- Restriction :  $Spec1$  and  $Spec2$  are input enable
- Hypothesis : Synchronous communication between  $IUT_1$  and  $IUT_2$  is supposed correctly implemented
- take a test purpose  $Obj$  for  $Spec$
- build  $Obj_{|Spec1}$  the test purpose for  $Spec1$  by projection of  $Obj$  on  $Spec1$
- test  $IUT_1$  with  $Obj_{|Spec1}$  as test purpose

# Testing refinement : *SpecC refines SpecA*

## Intuition



*SpecC refines SpecA*

iff all the traces of *SpecA* are traces of *SpecC*, up to the fact that actions introduced by the refinement step are forgotten

- Testing refinement : partial verification by selecting a finite number of traces of *SpecA*

## Key points

- Symbolically execution of a selected trace of *SpecA* on *SpecC*
- While executing the trace on *SpecC*, compute the associated path condition
- If *SpecC refines SpecA* then all path conditions have to be satisfiable with the same initial values for the attribute variables.