Introduction	Models	Encoding	Technology Transfer	Conclusion

# On the net encoding of asynchronous interactions

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Overview				

## General Theme

Relating calculi with asynchronous communication and Petri nets

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## Asynchronous calculi

#### Asynchronous process calculi

Formal models of distributed and concurrent systems with asynchronous communication [Honda, Tokoro'91], [Boudol'92]:

- no handshake between sender and receiver
- non-blocking send
- the message is sent, it travels to destination and it is (possibly) received

#### Observations

Only message sending is observable, reception is not

## Asynchronous calculi

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## Asynchronous CCS

CCS fragment of asynchronous pi-calculus

# Petri nets

#### Petri Nets

Widely used model of concurrent and distributed systems:

- formal semantics
- intuitive graphical representation

#### Asynchrony in Petri nets

Tokens are firstd generated by some transition and then consumed by others

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Relating asynchronous calculi and Petri nets

Can this intuitive correspondence between asynchronous calculi and Petri nets made formal?

## Open Petri nets

## Open Petri nets

Generalising Petri nets with composition and reactivity for modelling "open" systems

• interface / interaction with the environment through some designated places

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• composition between nets (using an interface)

# Open Petri nets

## Open Petri nets

Generalising Petri nets with composition and reactivity for modelling "open" systems

- interface / interaction with the environment through some designated places
- composition between nets (using an interface)

## Related ...

- Compositional semantics for Petri nets (SCONE, Petri box calculus, Petri Net algebra)
- Petri nets as reactive systems in the sense of Leifer, Milner ([Milner], [Sassone,Sobocinski])
- Workflows and web-service models (e.g., [van der Aalst])

# Results: Encoding asynchronous CCS into open nets

#### Encoding bounded asyncronous CCS into open nets

- it preserves structural congruence
- message exchanges as interactions at open places
- operational semantics: CCS reductions  $\leftrightarrow$  PN firings
- it preserves and reflects weak and strong bisimilarity

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## Results: Technology transfer on Expressiveness

Intimate connection between the two formalisms, useful for some technology transfer on expressiveness

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## Results: Technology transfer on Expressiveness

Intimate connection between the two formalisms, useful for some technology transfer on expressiveness

## Undecidability of bisimilarity (Strong/weak) bisimilarity for bounded asynchr. CCS is undecidable ↓ (Strong/weak) bisimilarity for open nets is undecidable

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## Results: Technology transfer on Expressiveness

Intimate connection between the two formalisms, useful for some technology transfer on expressiveness

## Undecidability of bisimilarity

(Strong/weak) bisimilarity for bounded asynchr. CCS is undecidable ↓ (Strong/weak) bisimilarity for open nets is undecidable

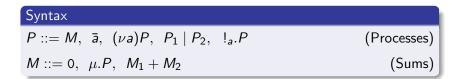
#### Decidability of convergence

Reachability is decidable for open Petri nets

Reachability/convergence is decidable for bounded asynchr. CCS

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Asynchro	nous CCS			

#### [Amadio,Castellani,Sangiorgi]



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#### [Amadio,Castellani,Sangiorgi]

# Syntax $P ::= M, \ \bar{a}, \ (\nu a)P, \ P_1 \mid P_2, \ !_a.P$ (Processes) $M ::= 0, \ \mu.P, \ M_1 + M_2$ (Sums)

#### Reduction semantics

$$a.P + M \mid \bar{a} \rightarrow P \qquad \tau.P + M \rightarrow P \qquad !_a.P \mid \bar{a} \rightarrow P \mid !_a.P$$

(+ usual structural axioms)

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## Asynchronous CCS: behavioral equivalences

#### Barb

Equivalence based on the notion of barb

 $P \downarrow \bar{a}$  if  $P \equiv \bar{a} \mid Q$ 

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## Asynchronous CCS: behavioral equivalences

#### Barb

Equivalence based on the notion of barb

$$P \downarrow \bar{a}$$
 if  $P \equiv \bar{a} \mid Q$ 

#### Barbed equivalence

A barbed bisimulation is a symmetric relation  $R \subseteq Proc \times Proc$  s.t. whenever  $(P, Q) \in R$  then

• if  $P \downarrow \bar{a}$  then  $Q \downarrow \bar{a}$ ,

2 if  $P \to P'$  then  $Q \to Q'$  and  $(P', Q') \in R$ .

Barbed bisimilarity  $\sim$  is the largest barbed bisimulation

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## Asynchronous CCS: equivalences

#### Barbed congruence

## $P \sim_b Q$ if $P \mid S \sim Q \mid S$ for all processes $S \in Proc$

## Asynchronous CCS: equivalences

#### Barbed congruence

$$P \sim_b Q$$
 if  $P \mid S \sim Q \mid S$  for all processes  $S \in Proc$ 

#### 1-bisimilarity

A 1-bisimulation is a symmetric relation  $R \subseteq Proc \times Proc$  s.t. whenever  $(P, Q) \in R$  then

$${f 0}$$
 if  $P o P'$  then  $Q o Q'$  and  $(P',Q')\in R$ ,

2 
$$\forall a \in \mathcal{N}. (P \mid \overline{a}, Q \mid \overline{a}) \in R$$

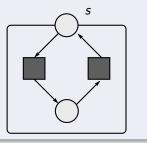
3) if 
$$P \equiv P' \mid \overline{a}$$
 then  $Q \equiv Q' \mid \overline{a}$  and  $(P', Q') \in R$ .

Strong 1-bisimilarity  $\sim_1$  is the largest strong 1-bisimulation

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Open nets				

#### Interface of the net

- open places
- the enviroment can put/remove tokens



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Open nets:	Behaviour			

Interactions at the interfaces / internal firing



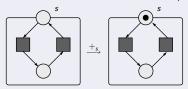
Weak and strong bisimilarities are totally standard

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Open nets:	Behaviour			

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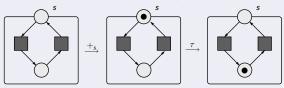
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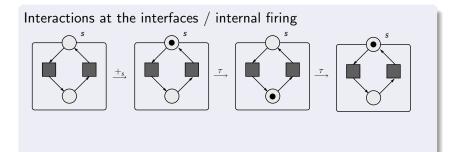


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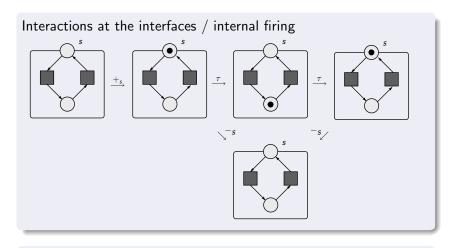
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#### Weak and strong bisimilarities are totally standard

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Weak and strong bisimilarities are totally standard

# Encoding asynchronous CCS into open nets

#### Bounded asynchronous CCS processes

The encoding is restricted to bounded processes: restriction never occurs under the scope of replication

 $!_a.(...(\nu b)(...)...)$  NO!!

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# Encoding asynchronous CCS into open nets

#### Bounded asynchronous CCS processes

The encoding is restricted to bounded processes: restriction never occurs under the scope of replication

$$!_a.(...(\nu b)(...)...)$$
 NO!!

#### Idea

- open places represent the free channels of a process
- messages represented by tokens in places
- transitions encode the control flow

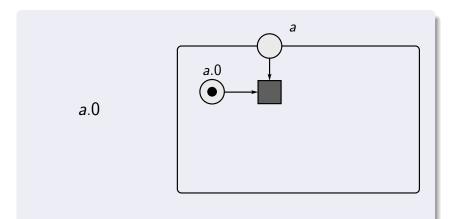
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Models

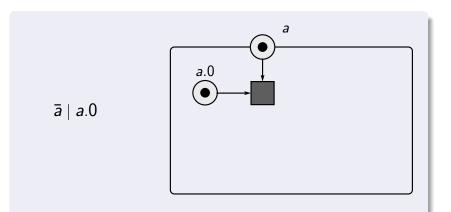
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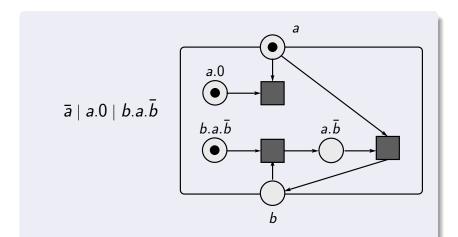


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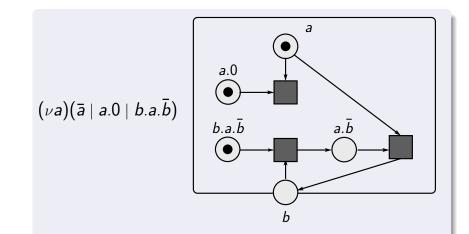


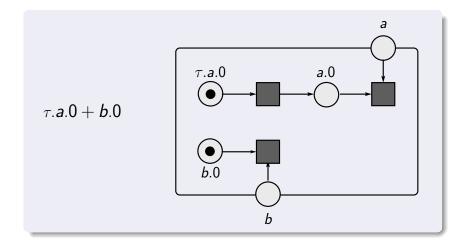
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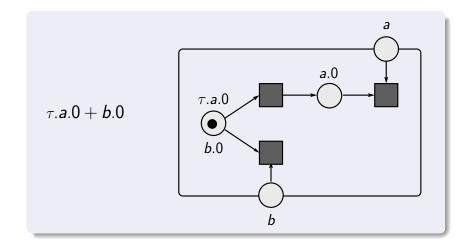


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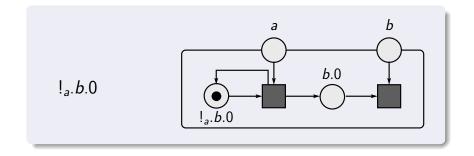




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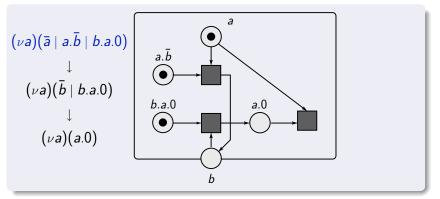
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Encoding: Replication





Any bounded asynchr. CCS process *P* encoded as an open net [*P*]

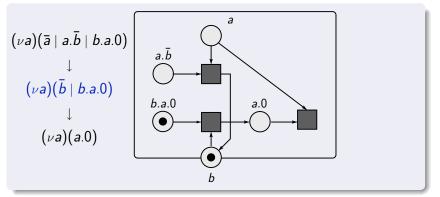
Any Q such that  $P \to^* Q$  corresponds to a marking  $\mathbf{m}(Q)$  of  $\llbracket P \rrbracket$ 





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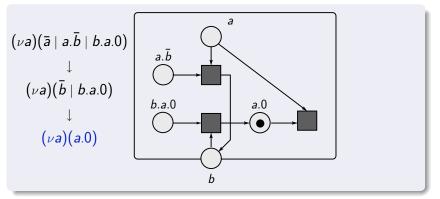
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#### Preservation and reflection of the operational semantics

For any bounded process P

 $P \rightarrow Q$  iff  $\mathbf{m}(P) \rightarrow \mathbf{m}(Q)$  in the open net  $\llbracket P \rrbracket$ 

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## Properties of the encoding

## Preservation and reflection of the operational semantics

For any bounded process P

$$P \to Q$$
 iff  $\mathbf{m}(P) \to \mathbf{m}(Q)$  in the open net  $\llbracket P \rrbracket$ 

Preservation and reflection of (strong/weak) bisimilarity

For any two bounded processes

$$P \sim Q$$
 iff  $\llbracket P \rrbracket \sim \llbracket Q \rrbracket$ 

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Technology Transfer

# Undecidability of bisimilarity

Undecidability of bisimilarity for bounded asynchronous CCS

- 2-register machines:
  - two integer registers r, s
  - program instructions: increment a register, jump on zero
- encoding 2-register machines as bounded aCCS processes
  - registers are represented as channels and their content as messages on such channels
  - zero testing can be only "weakly" simulated
- for any given machine we can construct two processes P and P' such that  $P \sim P'$  iff machine halts

 $\rightarrow$  bisimilarity on bounded asynchronous CCS is undecidable

As a consequence of the properties of the encoding ....

Corollary

Bisimilarity is undecidable for open Petri nets

#### Note

Outside the known undecidability results for PNs as we only observe interactions with the environment (all "traditional nets" are weakly bisimilar)

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## Convergence/reachability is decidable

Convergence in process calculi

A process *P* is called *convergent* if there is *Q* such that  $P \Rightarrow Q \not\rightarrow$ 

Reachability and presence of deadlocks is decidable for (open) nets  $\downarrow$ 

#### Corollary

Convergence is decidable for bounded asyncronous CCS

## Convergence/reachability is decidable

Convergence in process calculi

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#### Corollary

Convergence is decidable for bounded asyncronous CCS

#### More generally ...

For P, Q bounded processes, the problem

 $P|R \Rightarrow Q$  for some  $R = \bar{a}_1 \mid \ldots \mid \bar{a}_n$  is decidable

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Conclusions	:			

Tight relation between asynchronous CCS and open Petri nets, exploited for a technology transfer in expressiveness

#### Generalisation to full CCS and pi-calculus

Infiniteness of channels and variable topology. Open dynamic nets? Open GTSs?

#### Concurrent sematics

- well-understood for open Petri nets
- few studies for asynchronous calculi

#### Step equivalences

Weak concurrent equivalences coincide with non-concurrent ones: intriguing connection between concurrency and asynchrony

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