Shadows of diagrams and Euler-Zagier sums

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Abstract. We

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1. Introduction

2. The deformed algebra of labelled diagrams

2.1. How these diagrams arise

2.2. Codings and the deformed algebra

2.3. LBELL

3. Euler-Zagier sums

3.1. Definitions

3.2. Shadows and interpretations

3.3. General picture

4. Conclusion

Discuss the self-dual deformation.

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